

所 別：工程技術研究所
學程別：自動化及控制學程

組別：丙組

科目：控制系統

工程技術研究所 自動化及控制學程

碩士班入學考試 Control System 試題 April 1997

1. Give the comparison of an open-loop control system and closed-loop control system on construction, cost, stability, sensitivity, and effect of external disturbance. (10%)

2. Consider a closed-loop system shown in figure 1.

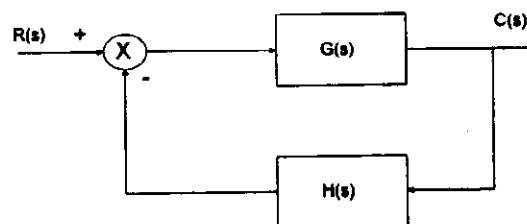


Figure 1.

where $G(s) = \frac{10(s+1)}{s(s-3)}$ and $H(s) = 1$

- (1) What are the closed-loop poles and zero? (3%)
- (2) Sketch the root locus. (7%)
- (3) Find the unit-step response $c(t)$. (7%)
- (4) Calculate $c(t)$ at $t = 0, 1, \infty$ (3%)

3. Sketch the root locus of a closed-loop system with unity feedback gain as shown in figure 1.

where $G(s) = \frac{64k}{s(s+4)(s+16)}$, $H(s) = 1$ and $E(s) = R(s) - C(s)$

- (1) Sketch the root locus. (7%)
- (2) Determine the range of k for which the system is stable. (5%)
- (3) Determine the range of k such that the steady state error $e(t)$ is less than 0.1 with a ramp input $r(t) = t, t > 0$. (5%)
- (4) Find the steady state error $e(t)$ for an unit-step input $r(t) = 1, t > 0$. (3%)

4. For a transfer function $G(s) = \frac{C(s)}{U(s)} = \frac{s+4}{s^3 + 6s^2 + 11s + 6}$

Transfer to a state model $\dot{X} = AX + BU$ and draw the signal-flow graph using nodes u, x_3, x_2, x_1, c , etc. (15%)

所 別：工程技術研究所
學 程 別：自動化及控制學程

組 別：丙組

科 目：控制系統

5. Outline the methods for the determination of the stability of linear continuous-data system, without involving root solving. (15%)

6. Consider that an open-loop transfer function of a control system with unity feedback is given by $G(s) = \frac{k}{s(1 + 0.02s)(1 + 0.2s)}$ and the bode plot of $G(s)$ is shown in figure 2. From the graph, the magnitude of $G(j\omega)$ at the phase-crossover frequency 15.88 rad/s is -14.82 dB, and the phase of $G(j\omega)$ at gain-crossover frequency 6.22 rad/s is -142.28 degrees.

- (1) Find the gain margin ,phase margin, the value of k and check the system stability.(6%)
- (2) Sketch the Nyquist plot.(6%)
- (3) Estimate the gain margin ,phase margin and check the system stability for $k=1$ (4%)
- (4) Estimate the gain margin ,phase margin and check the system stability for $k=100$ (4%)

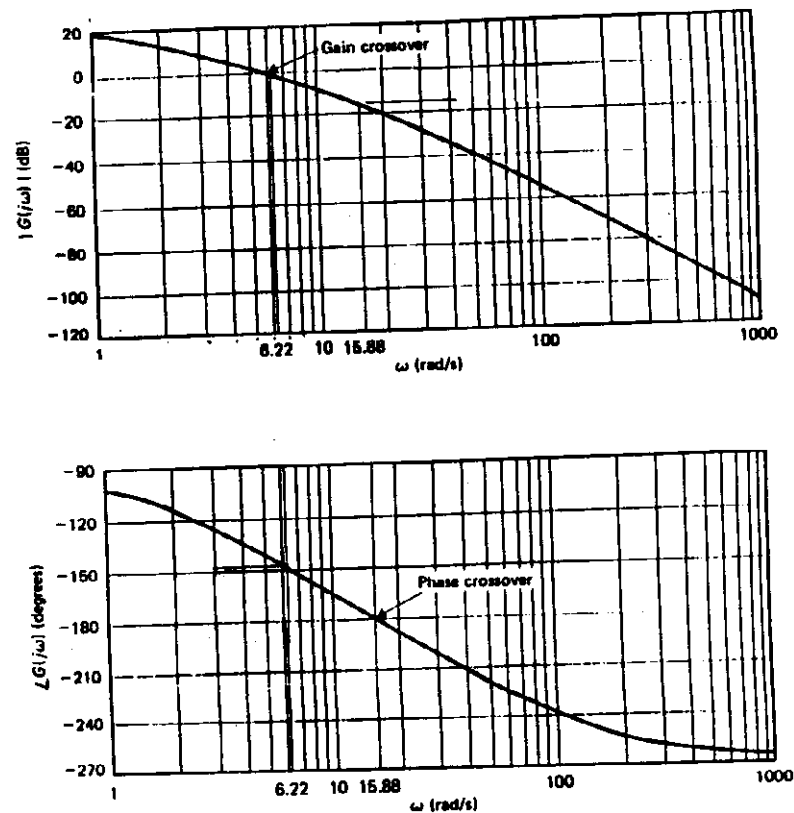


Figure 2. Bode plot of $G(s) = k/[s(1+0.02s)(1+0.2s)]$