

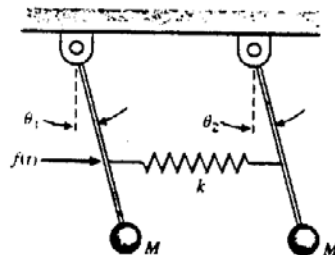
國立臺灣科技大學  
八十八學年度碩士班招生考試試題

系所別：纖維及高分子工程研究所

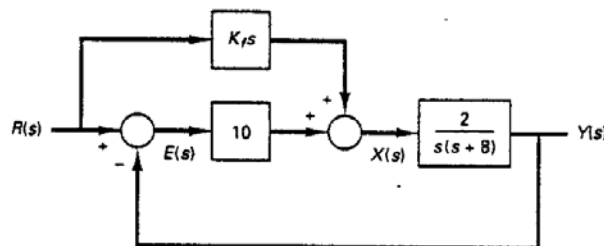
組別：丙組

科目：控制系統

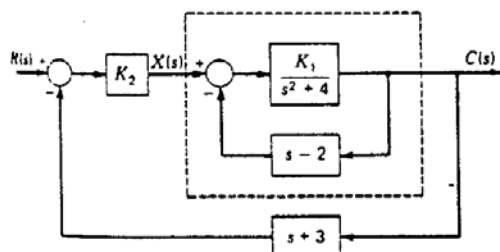
1. Two pendulums are suspended from frictionless pivots and connected at their mid-points by a spring. Assume that each pendulum can be represented by a mass  $M$  at the end of a massless bar of length  $L$ . Also assume that the displacement is small and linear approximations can be used for  $\sin\theta$  and  $\cos\theta$ . The spring located in the middle of the bars is unstretched when  $\theta_1 = \theta_2$ . The input force is represented by  $f(t)$ , which influences the left-hand bar only. The moment of inertia for a pendulum about the pivot is given by  $J = ML^2$ . Determine the transfer function  $T(s) = \theta_1(s)/F(s)$ . (15%)



2. Consider the following feedforward system. Determine  $K_f$  such that the steady-state error is zero with a ramp input of  $1.0t$ . (15%)



3. The portion of the system enclosed by the dashed box in the following figure represents the plant to be controlled. For  $K_1 = 2$ , construct the root-locus plot for the entire system,  $0 < K_2 < \infty$ . For what values of  $K_2$  does the system have an oscillatory response? What is the smallest possible damping ratio? (20%)



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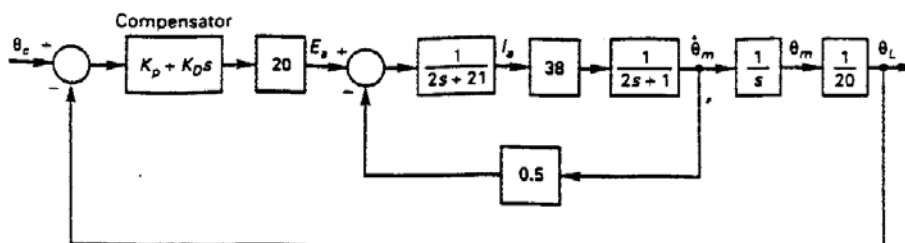
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Shown in Figure is the control system for one joint of a robot arm. The controller is a PD compensator, with  $G_C(s) = (K_P + K_D s)$ .  $K_P$  is the proportional gain and  $K_D$  is the derivative gain.



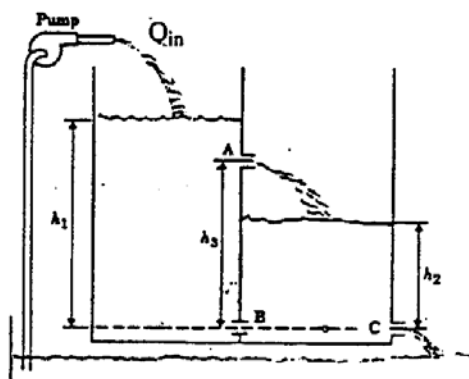
Joint control system for robot arm.

(a) Find the transfer function  $\frac{\theta_L(s)}{E_a(s)}$ . (15%)

(b) As a first step in the system design, determine all possible values for the coefficients  $K_P$  and  $K_D$ , which add a zero to the system at  $s = -2$  and simultaneously stabilize the system. (10%)

5

A sketch of a laboratory experiment in a fluid (water) flow is shown in the figure below with the inflow rate  $Q_{in}$ .



Assume that the flow through the equal-sized holes A, B and C is described by

$$Q = K \sqrt{P_{in} - P_{out}}, \text{ where } Q \text{ is the flow rate, } K \text{ is the constant, } P \text{ is the pressure.}$$

With holes at A and C and no hole at B, write the equations of motion for this system in terms of  $h_1$  and  $h_2$ . Assume that  $h_3$  is 20 cm and  $h_2$  is less than 20 cm. When  $h_2$  is 10 cm, the outflow is 200 cm<sup>3</sup>/min. Compute the constant  $K$  and include it in your equations. (15%)

6

Can a right-half s-plane pole of a plant be effectively cancelled by a compensator with a right-half s-plane zero? Why? (10%)