

國立臺灣科技大學
九十一學年度碩士班招生考試試題

系所組別：電子工程系乙一組
科目：通信系統

(總分 100 分)

1.

(a) $x(t) = \sin ct$ is the input to a system with impulse response $h(t) = \text{sinc}^2 t$, plot the spectrum of the output signal $y(t)$. (5%)

(b) Define $k(t) = \sum_{m=-\infty}^{\infty} \delta(t - mT)$ and let $p(t) = y(t)k(t)$. Given that $T = 1 \text{ sec}$, plot the spectrum of $p(t)$. (5%)

(c) $j(t)$ is shown in Fig. 1. $j(t)$ is a periodic pulse train with width T . Given $T_s = 0.5 \text{ sec}$ and let $q(t) = y(t)j(t)$, plot the spectrum of $q(t)$. (You need to present the detail calculation) (15%)



Fig. 1

2.

(a) A binary communication system transmits signals $s_i(t)$ ($i=1, 2$). The receiver test statistic $z(T) = a_i + n_0$, where the signal component a_i is either $a_1 = +1$ or $a_2 = -1$ and the noise component n_0 is uniformly distributed, yielding the conditional density functions $p(z|s_i)$ given by

$$p(z|s_1) = \begin{cases} \frac{1}{2} & \text{for } -0.2 \leq z \leq 1.8 \\ 0 & \text{otherwise} \end{cases}$$

and

$$p(z|s_2) = \begin{cases} \frac{1}{2} & \text{for } -1.8 \leq z \leq 0.2 \\ 0 & \text{otherwise} \end{cases}$$

Find the probability of a bit error, P_b , for the case of equally likely signaling and the use of an optimum decision threshold. (10%)

(b) Repeat problem (a) with the following changes.

n_0 is Gaussian noise.

$$p(z|s_1) = \frac{1}{\sigma_0 \sqrt{2\pi}} \exp\left(-\frac{1}{2} \left(\frac{z - a_1}{\sigma_0}\right)^2\right)$$



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$$p(z|s_2) = \frac{1}{\sigma_0 \sqrt{2\pi}} \exp\left(-\frac{1}{2} \left(\frac{z - a_2}{\sigma_0}\right)^2\right)$$

$$p(s_1) = p, \quad p(s_2) = q$$

Find the optimum decision threshold that minimize P_e . (10%)

3. A desired impulse response of a communication system is the ideal $h(t) = \delta(t)$, where $\delta(t)$ is the impulse function. Assume that the channel introduces ISI so that the overall impulse response becomes $h(t) = \delta(t) + \alpha\delta(t - T)$, where $\alpha < 1$, and T is the symbol time. Derive an expression for the impulse response of a zero-forcing filter that will equalize the effects of ISI. Demonstrate that this filter suppresses the ISI. (15%)

4. Find the probability of bit error P_b for the coherent matched filter detection of the equally likely binary FSK signals

$$s_1(t) = 0.5 \cos 2000\pi t$$

and

$$s_2(t) = 0.5 \cos 2020\pi t,$$

where the two-sided AWGN power spectral density is $N_0/2 = 0.0001$. Assume that the symbol duration is $T = 0.01s$. (15%)

5. Suppose that the message signal is given as

$$m(t) = 10 + 4 \cos 2\pi t + 8 \cos 4\pi t + 10 \cos 20\pi t$$

Specify the frequency-response characteristic of a VSB filter that passes the upper sideband and first frequency component of the lower sideband. (10%)

6. Two independent white Gaussian noise with power spectral density $\frac{N_1}{2}$,

$$\frac{N_2}{2} \text{ are fed to } H_1(f) = \left(1 + j \frac{f}{f_1}\right)^{-1} \text{ and } H_2(f) = \left(1 + j \frac{f}{f_2}\right)^{-1}$$

respectively. Let $x(t), y(t)$ be the output for $H_1(f)$ and $H_2(f)$.

(a) Find $R_x(\tau)$. (5%)

(b) Let $z(t) = x(t)y(t)$, find the power spectral density $S_z(f)$. (10%)

